

On the Geomechanics of Induced Seismicity

Neal B. Nagel, Ph.D. May 9, 2017

Outline

- 1. Introduction
- 2. Geomechanics
- 3. Stress/Strain
- 4. Stress & Pressure
- 5. Faults & Fractures
- 6. Oklahoma Case History



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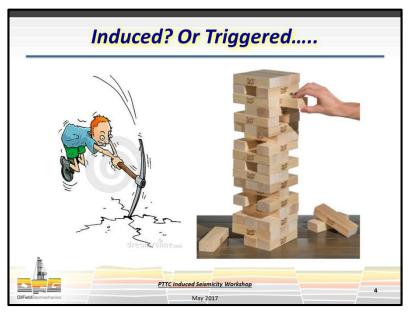
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INTRODUCTION

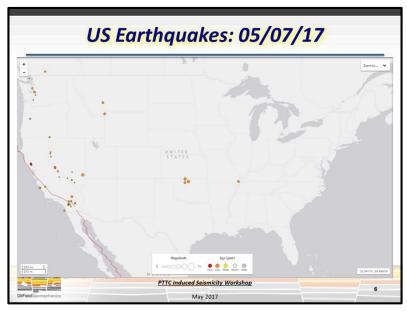


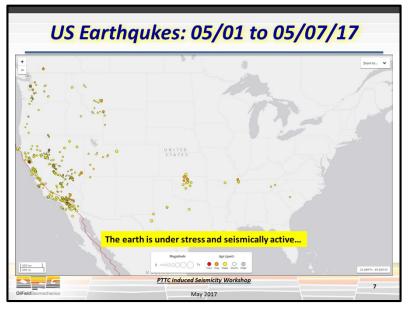
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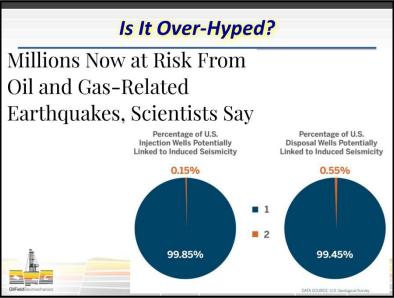
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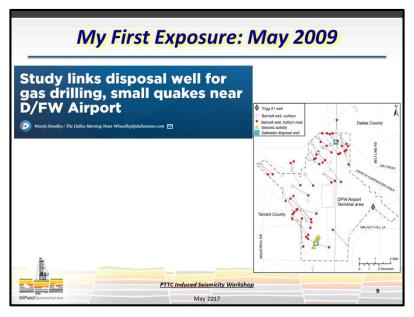


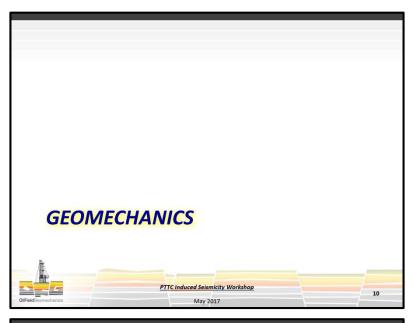


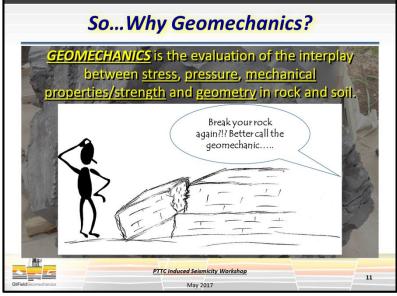


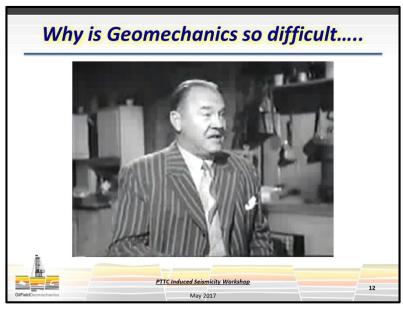




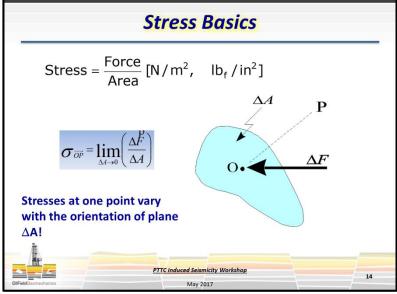


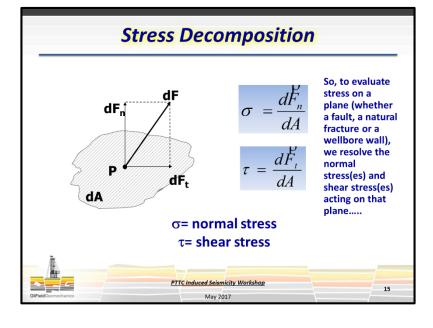












Stress

- Stress, in units of psi or MPa, is simply: Stress=Force/Area=F/A
- Normal stress is defined as:

$$\sigma_n = \lim_{\Delta A \to 0} \frac{\Delta F_n}{\Delta A}$$

• Shear stress is defined as: $\tau_n = \lim_{n \to \infty} \frac{1}{n}$

$$\tau_n = \lim_{\Delta A \to 0} \frac{\Delta F_t}{\Delta A}$$

- Key concepts:
- The general convention is that "compressive" stress is positive, "tensile" stress is negative.
- Stress is a tensor (requiring 3 independent normal and 3 independent shear values).
- A "Principal" stress occurs in an orientation where the shear stress is zero. Three principal stresses exist in an orthoginal orientation.
- "Plane" stress occurs when both the normal and shear stresses in one orthoginal direction are zero.
- "Lithostatic" stress is the stress due to the weight of the overburden. "Hydrostatic" stress is when all three principal stresses are equal.



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Strain

- Strain, dimensionless (in/in or %), is the deformation of a body in response to a change in stress: Strain=DL/L
- Normal strain is defined as: $\varepsilon = \lim_{\Delta L \to 0} \frac{\delta L}{\Delta L}$
- Shear strain is defined as: $\gamma = TAN(\alpha)$
- Key concepts:
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 - "Plane" strain occurs when both the normal and shear strains associated with one orthoginal direction are zero.

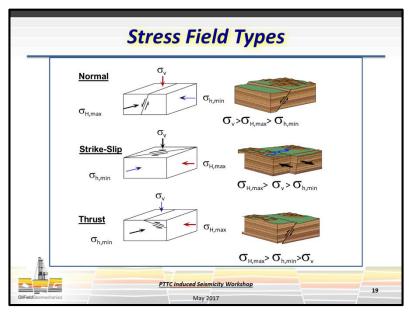


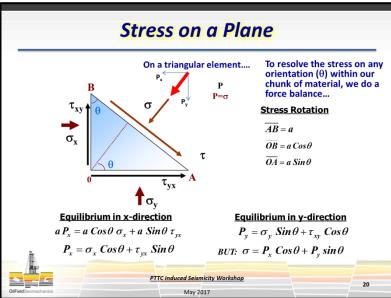
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Stress on a Plane

Normal stress acting on the plane:

$$\sigma = \sigma_x \cos^2 \theta + 2\tau_{xy} \sin \theta \cos \theta + \sigma_y \sin^2 \theta$$

Shear stress acting on the plane:

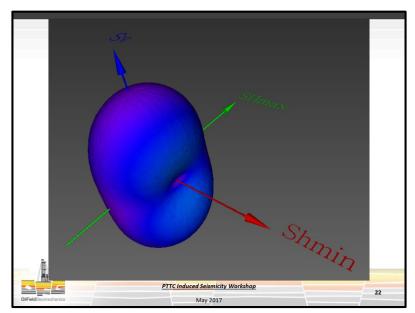
$$\tau = \frac{1}{2} (\sigma_y - \sigma_x) \sin 2\theta + \tau_{xy} \cos 2\theta$$

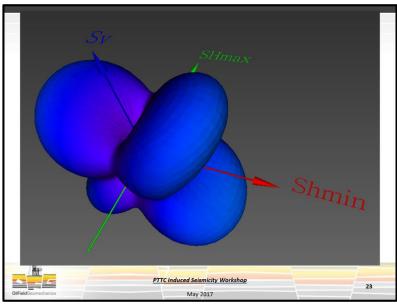
Principal stresses (acting normal to a plane where $\tau = 0$):

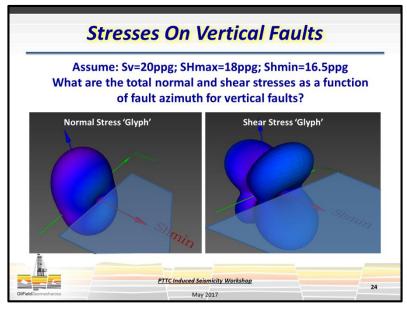
$$\sigma_{1,2} = \frac{1}{2} \left(\sigma_x + \sigma_y \right) \pm \sqrt{\tau_{xy}^2 + \frac{1}{4} \left(\sigma_x - \sigma_y \right)^2}$$



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Assume: Sv=20ppg; SHmax=18ppg; Shmin=16.5ppg What are the total normal and shear stresses as a function of fault dip direction (SHmax_Az=0°)? Shear Stress (ppg): Vertical Natural Fractures Official Normal Stress: Vertical Natural Fractures Dip Direction PTTC Induced Seismicity Workshop May 2017



Poroelasticity

- Largely, the concepts just presented assume that the material is homogeneous and solid. Rock, however, is inhomogeneous and filled with fluids.
- Pore fluids can, and do, play a major role in the constitutive behavior of rock.
- "Poroelasticity", the elastic behavior of porous material, is based upon the work of Maurice Biot.
- In addition, Karl Terzaghi developed the concept of "effective stress".



Effective Stress

 Terzaghi realized that, for soils, it was not the total stress that soils responded to but the stress acting on the soil particles themselves:

Effective Stress,
$$\sigma'_{ij} = \sigma_{ij} - p_o \delta_{ij}$$

where p_o is pore pressure, δ is the Kronecker delta, and i and j are axes designations.

For rocks, this has been simplified to:

$$\sigma'_{ij} = \sigma_{ij} - \alpha p_o$$

where α is Biot's constant and is ~ 1 (and is related to the ratio of the frame modulus to the solid modulus).



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Effective Stress

- The practical consequence of the effective stress principle is that rock behavior is governed not only by the total stresses acting, but also the fluid pressures acting.
- Further, this suggests that in situations where we do not change the total stresses (say, deep in the earth) but do change pore pressure, we can cause a significant behavioral response from the rock and even failure.

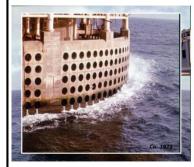


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North Sea Subsidence







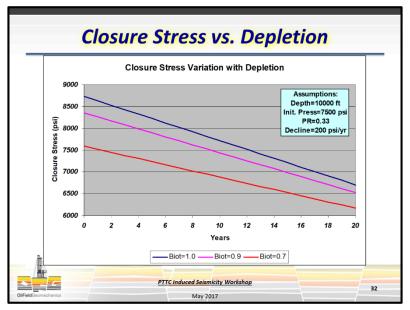
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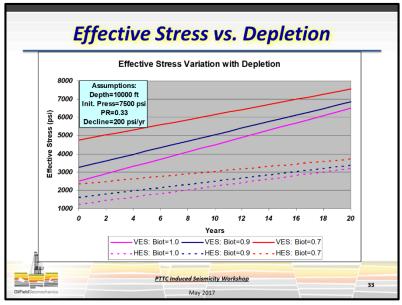
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Closure Stress or Frac Gradient

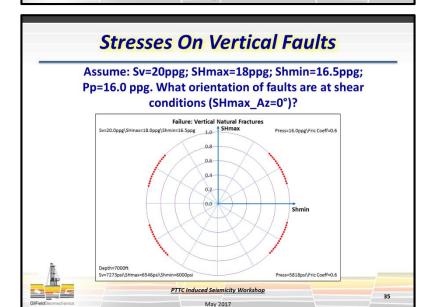
- Closure Stress or FG, which is taken to be the stress at which a fracture closes (or opens, actually), is, ideally, the far field total minimum horizontal stress, Shmin (i.e., the sum of the effective stress and pore pressure).
- What happens as the formation pressure changes over time? Does the Shmin stress change? Increase? Decrease?







Assume: Sv=20ppg; SHmax=18ppg; Shmin=16.5ppg; Pp=16.0 ppg. What are the normal and shear stresses as a function of fault dip direction (SHmax_Az=0°)? Shear Stress (ppg): Vertical Natural Fractures PTTC Induced Seismicity Workshop



Conditions for Fault Slip (EQs!!)

Normal Effective Stress x Friction Coefficient < Shear Stress

$(\sigma_{Tn}-P_p) \times tan(\phi) < \tau$

 σ_{Tn} =Total normal stress on fault;

P_p = Pressure on fault plane;

 Φ = Friction angle; and

 τ = Shear stress on fault plane.



Normal and Abnormal Pressure

- <u>Normal pressure</u> is defined as the condition where the fluid pressure equals the hydrostatic pressure of seawater (open system).
- Abnormal pressure is a condition where the fluid pressure is greater than the hydrostatic fluid pressure for seawater (closed system).
- <u>Subnormal pressure</u> is the condition where the fluid pressure is less than the hydrostatic pressure for seawater (how might this occur?).

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Pressure, psi

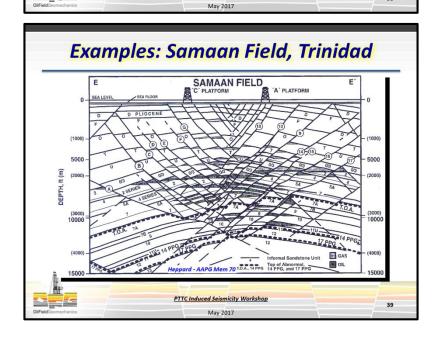
Pressure, psi

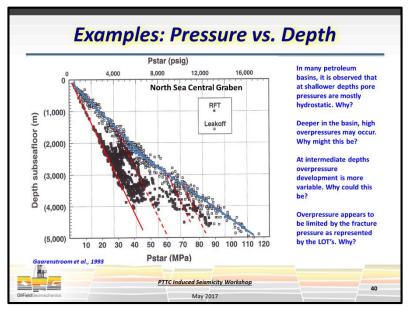
Pressure Gradient, psi/ft

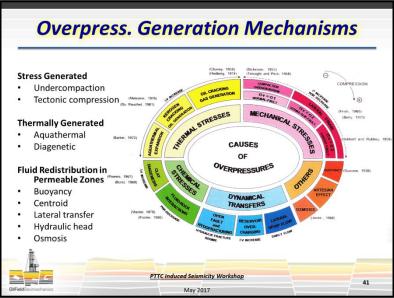
Salt 0.465 psi/ft, 1.07 gm/cc

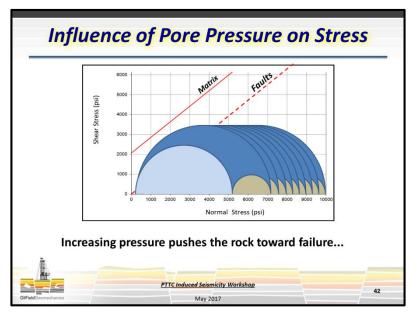
Fresh 0.433 psi/ft, 1.07 gm/cc

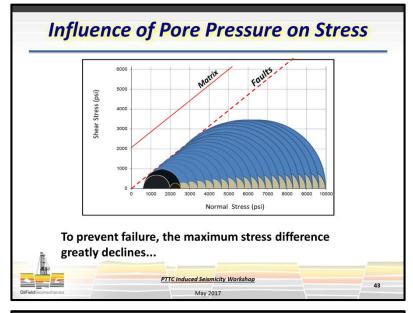
Fresh 0.433 psi/ft, 1.0 gm/cc

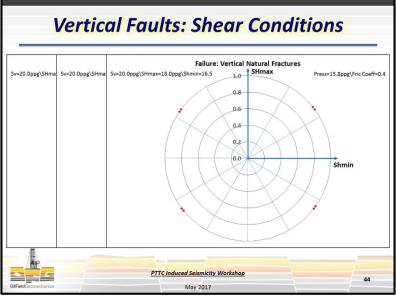


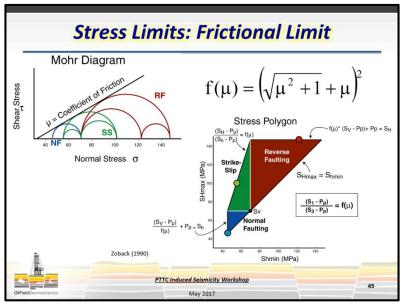








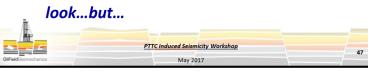


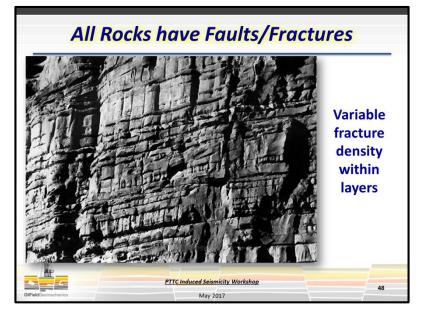


FAULTS & FRACTURES PTTC Induced Seismicity Workshop ONFeld Surmechanics May 2017

Rock Irrefutable Realities...

- 1. All rocks have fractures...
- 2. Fractures are created/reactivated by stresses...
- 3. We can never know exactly how many fractures, where are they and how they look...but...





Properties of Faults/Fractures

The hydro-mechanical behavior of the joint is controlled primarily by the roughness of the surface

Using the words favored by Professor Neville Cook:

"Natural joints in rock can be described as two rough surfaces in partial contact"

The roughness of the joint surfaces depends on many factors: rock type and the geological conditions to which the joint has been subjected.

All surfaces are rough on some scale and that the contact between two rough surfaces affects most physical properties, including electrical and thermal conductance, stiffness, strength, and hydraulic conductivity.



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Mechanical Properties-Dilation

Before mechanical test





After mechanical test

Samples from TASQ tunnel at Äspö HRL Normal loading and shear tests on joints

Lars Jacobsson, Mathias Flansbjer

SP Swedish National Testing and Research Institute
Bode Sweden



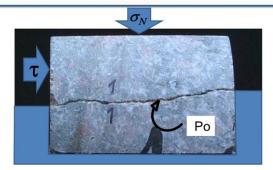


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Natural Fracture Mechanical Behavior



Effective stress= σ' Total stress= σ_N Pore pressure=Po

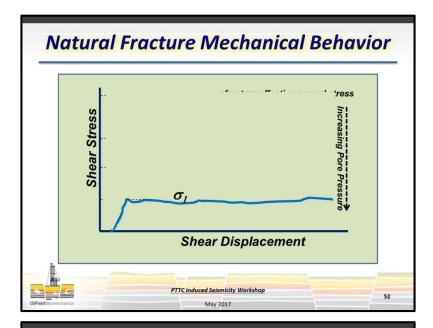
$$\sigma' = \sigma_N - p_a$$



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What Are Common Characteristics?

- > Very non-linear mechanical behavior.
- > Shearing damage.
- Normal stiffness dependence on normal stress; and
- Decrease in dilation angle with plastic shear displacement.



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Flow and Deformation of Fractures

The direct relationship between fluid flow and fracture aperture has been established from experimental, theoretical, and numerical investigations of fluid flow through a fracture.

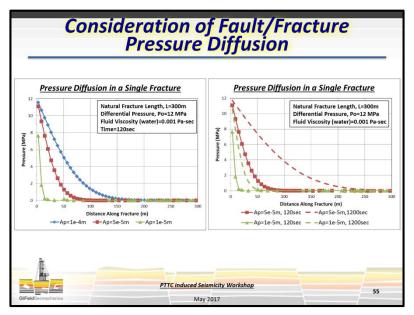
The cubic law:
$$Q = \frac{\gamma_w}{12\mu} Ga^3 \Delta h$$

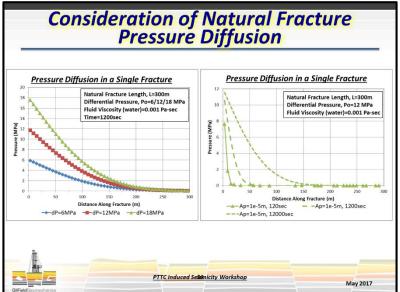
Aperture	Flow
100%	100%
90%	73%
70%	34%
50%	13%

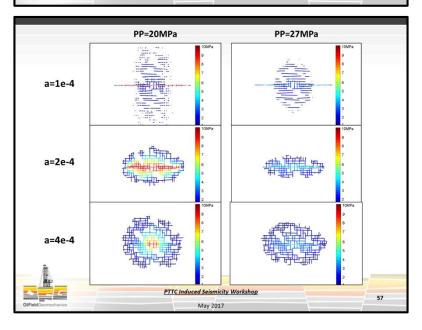
This relationship is the Reynolds equation for viscous flow between parallel plates and is often referred to as the cubic law.

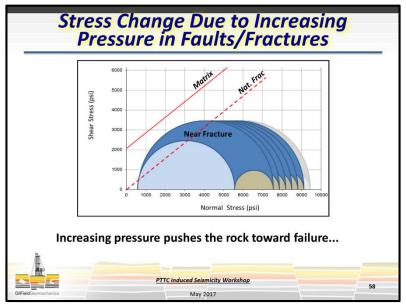


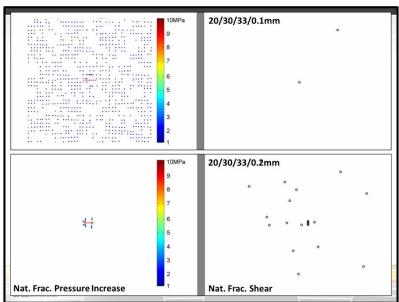
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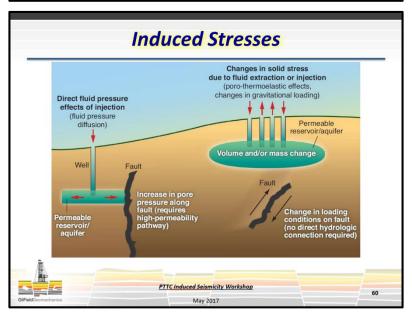


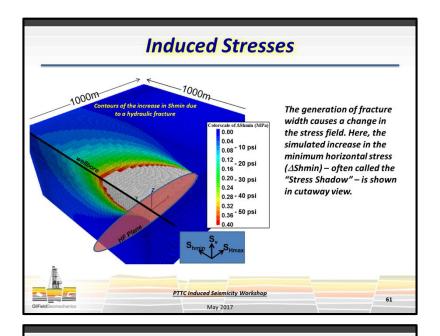












KEY ISSUES

Base Data:

- 1. Initial stress field magnitude, orientation, ranking
- 2. Initial pressure field over/under/normal pressure
- 3. Fault/fracture structure dip, dip direction, length, connectivity
- Fault/fracture mechanical properties friction, cohesion, aperture, permeability

Operational Effects:

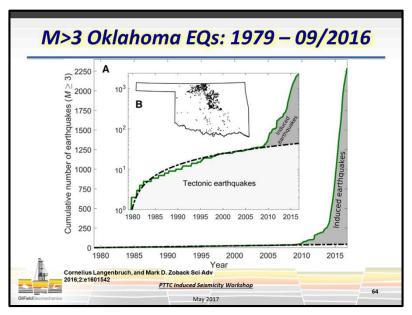
- 1. Induced pressure changes injection, poro-elastic
- 2. Induced stress changes loads, deformations, pressures

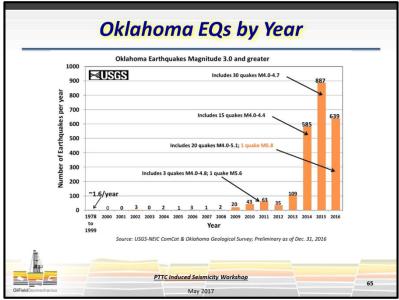
Injection Parameters:

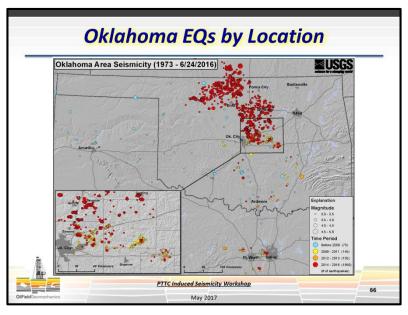
1. Injection parameters - location

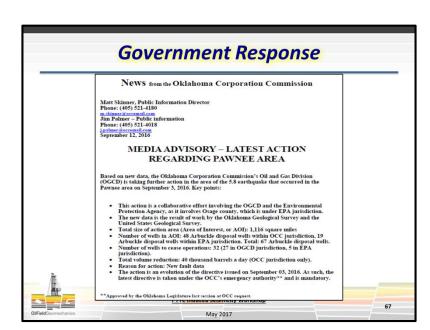


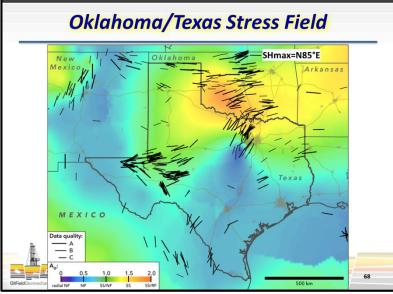
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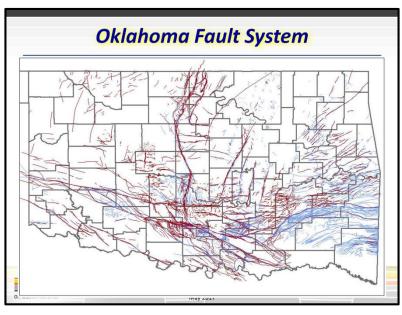


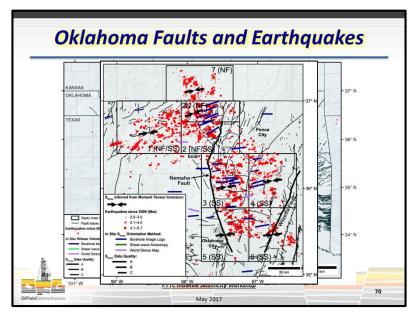


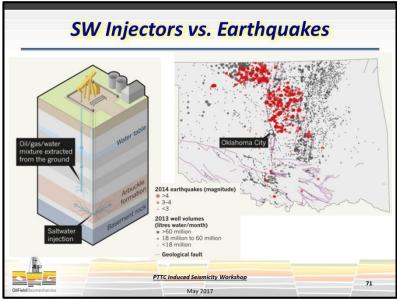


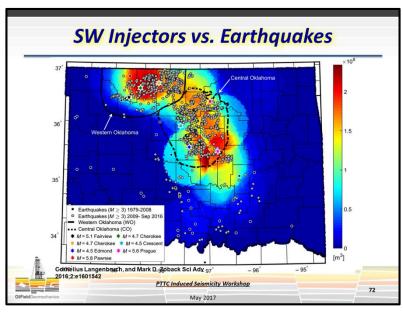


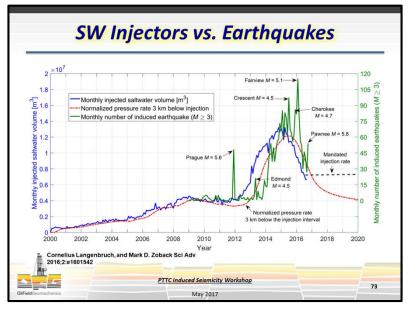


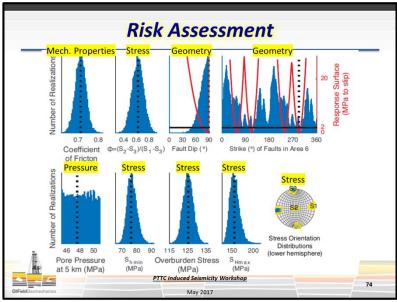


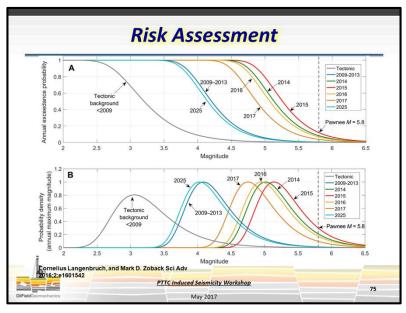


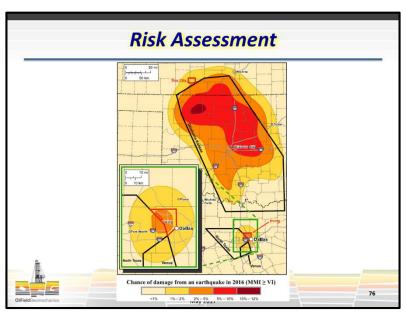


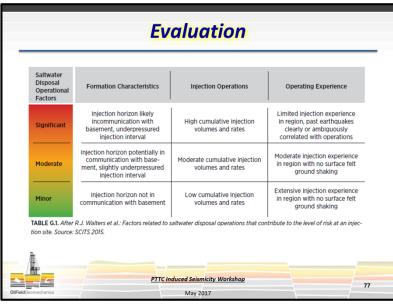












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Neal Nagel, Ph.D.
Chief Engineer, Oilfield Geomechanics LLC (OFG)
Rosenberg, Texas 77471
www.ofgeomech.com

832-327-9566

